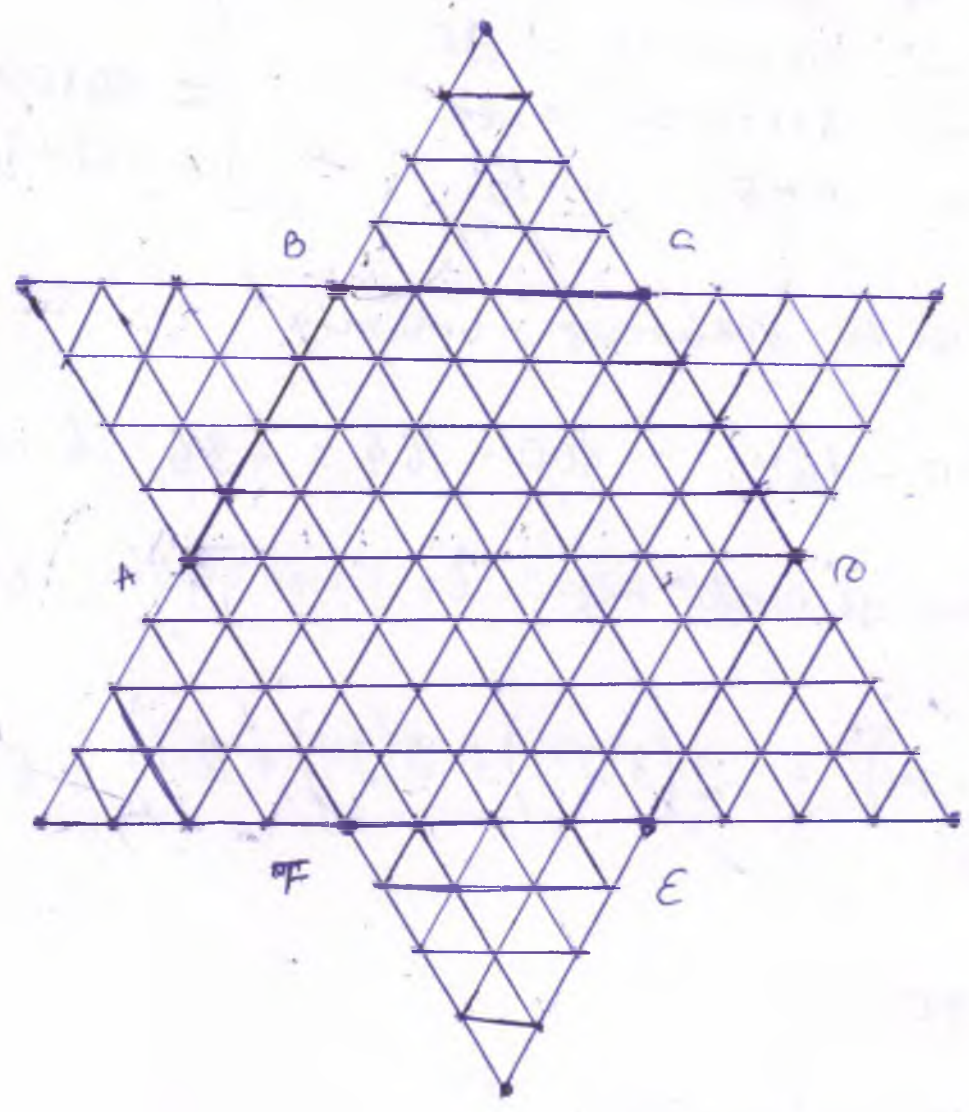


1



1-bölib. eng katta 1 ta uchburclak, ichidagilar ni hisoblaymiz.

Tomoni	Uzunligi	Hisoblash	Yig'indisi
1	1	$1 \cdot 2 + 2 \cdot (1+2+\dots+11) = 144$	→ 210 ←
2	2	$1+2+\dots+11 = \frac{11 \cdot 12}{2} = 66$	
3	3	$1+2+\dots+10 = \frac{10 \cdot 11}{2} = 55$	→ 100 ←
4	4	$1+2+\dots+9 = \frac{9 \cdot 10}{2} = 45$	
5	5	$1+2+\dots+8 = \frac{8 \cdot 9}{2} = 36$	→ 85 ←
6	6	$1+2+\dots+7 = \frac{7 \cdot 8}{2} = 28$	
7	7	$1+2+\dots+6 = \frac{6 \cdot 7}{2} = 21$	→ 25 ←
8	8	$1+2+\dots+5 = \frac{5 \cdot 6}{2} = 15$	
9	9	$1+2+\dots+4 = \frac{4 \cdot 5}{2} = 10$	→ 10 ←
10	10	$1+2+\dots+3 = \frac{3 \cdot 4}{2} = 6$	
11	11	$1+2 = \frac{2 \cdot 3}{2} = 3$	→ 10 ←
12	12	$1 = 1 = 1$	

**= 330**

end: ABCDEF — 6 ta burchak ichidagi  $\Delta$ larni sanaymi

1	$\rightarrow$	96 ta	] $\begin{aligned} &= 96 + 36 + 22 + 10 = \\ &= 132 + 32 = \underline{164 \text{ ta}} \end{aligned}$
2	$\rightarrow$	$5+6+7+6+5 = 36$	
3	$\rightarrow$	$5+6+6+5 = 22$	
4	$\rightarrow$	$5+5 = 10$	

demak 164 ta uchburchak umumiy

$$300 + 300 - 164 = 600 - 164 = 436 \text{ ta uchburchak}$$

Endi qo'shgan chiziq larimizni, 6 ta ichiga olgan  $\Delta$ larni

Sanaymiz

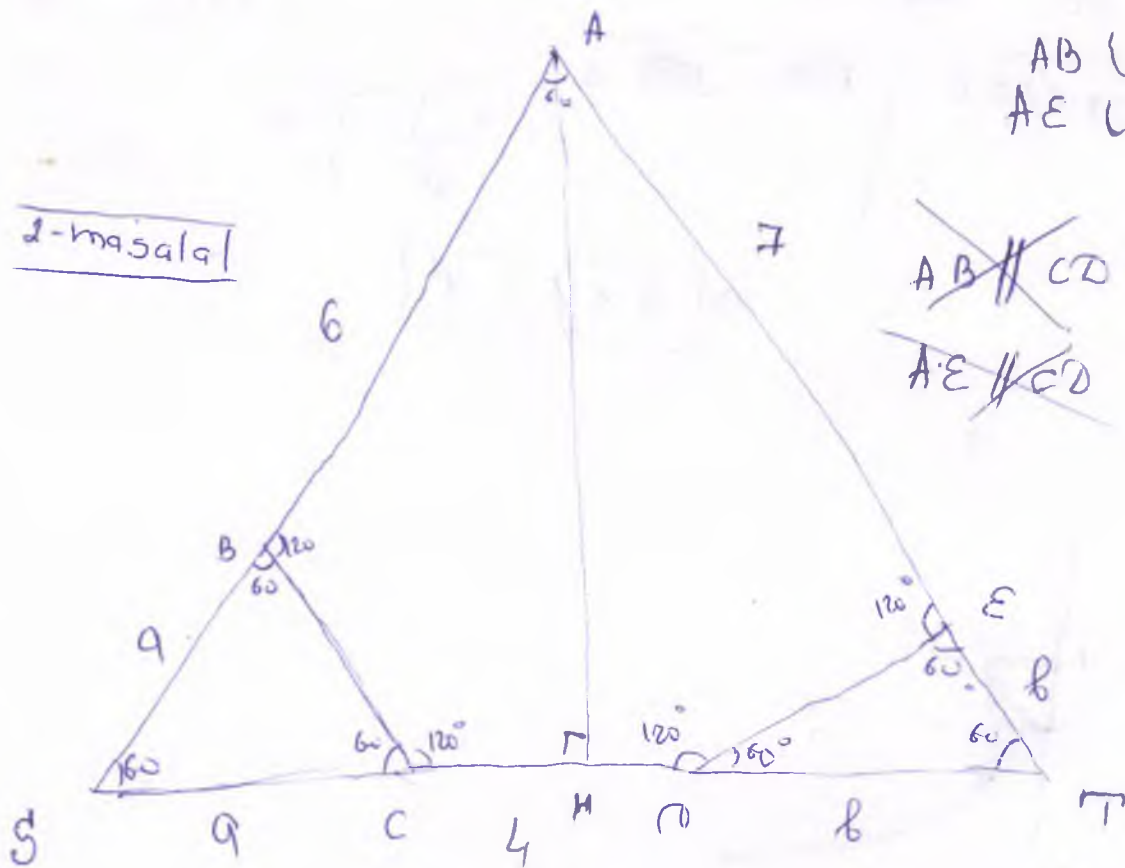
$$6 \left( 2 \cdot (4+3+2+1) + 2(3+2+1) + 2(2+1) + 2 \cdot 1 \right) = 6 \cdot 2(10+6+3+1)$$

$$= 12 \cdot 20 = 240$$

$$\text{Shunda } 436 - 240 = \boxed{236} \text{ ta}$$

J: 236

2-masala



$$AB \cup CD = S$$

$$AE \cup CD = T$$

~~$AB \parallel CD \Rightarrow \text{chunki } \angle ABC + \angle BCD \neq 180$~~

~~$AE \parallel CD \Rightarrow \text{chunki } \angle AED + \angle EDC \neq 180$~~

$$180^\circ - \angle ABC = \angle CBS' = 60^\circ$$

$$180^\circ - \angle BCD = \angle BCS' = 60^\circ$$

$\Rightarrow \Delta BSC \rightarrow \text{muntazam}$

xyddi shunday  $\Delta DET \rightarrow \text{muntazam}$

$\Delta AST$  e muntazam

$$\begin{aligned} \Rightarrow BS' = SC = 9 \\ \Delta T = TE = b \end{aligned} \quad \left| \quad \begin{aligned} a+6 = b+7 \Rightarrow \\ a+6 = a+b+4 \Rightarrow \end{aligned} \right. \quad \begin{aligned} a = b+1 \\ b = 2 \end{aligned} \quad \left| \quad \begin{aligned} a = 3 \\ b = 2 \end{aligned}$$

Demak  $AS' = ST' = AT' = 9$

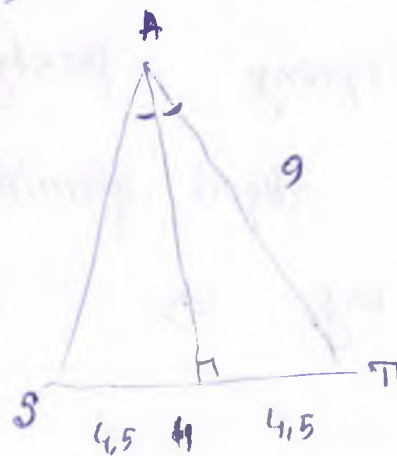
AH  $\rightarrow$  balandlik, bissek-trisa, mediana

$$\Rightarrow AH^2 = HT^2 + AT^2 = (4,5)^2 + 9^2 =$$

$$= 20,25 + 81$$

$$AH^2 = 100,25$$

$$AH = \sqrt{100,25} = \frac{\sqrt{401}}{2}$$



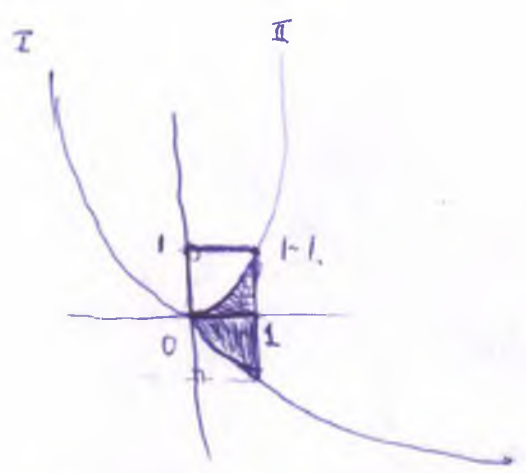
$$J: \frac{\sqrt{401}}{2}$$

3.  $(y + \sqrt{x})(y - x^2)\sqrt{1-x} \leq 0$  tenglikda  $\sqrt{x}, \sqrt{1-x}$ , bor  $\Rightarrow$   $\begin{matrix} x \geq 0 \\ x \leq 1 \end{matrix} \Rightarrow 0 \leq x \leq 1$

$\sqrt{1-x} \geq 0 \Rightarrow (y + \sqrt{x})(y - x^2) \leq 0$   $\Rightarrow$   $\frac{+}{-\sqrt{x}} \quad \frac{-}{x^2} \quad \frac{+}{+}$

$\Rightarrow \boxed{-\sqrt{x} \leq y \leq x^2}$

$y = x^2$   
 $y = -\sqrt{x}$



$y = \sqrt{x}$  va  $y = -\sqrt{x} \Rightarrow x = y^2$  demak  $y = -\sqrt{x}$  funksiya  
 $y = x^2$  funksiyani 2-qismiga teng.

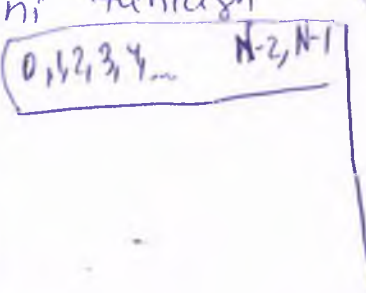
$\Rightarrow y = x^2$  funksiyani ~~2-qismiga~~ 2 qismini  $90^\circ$  ga burusak  
 $y = -\sqrt{x}$  funksiya hozir bo'lad.

$\Rightarrow$  x o'qining pastgi qismidagi bo'yalgan yuz,  
x o'qining yuqori qismidagi ajratib ko'rsatilgan bo'yalmasan  
yuzga teng  $\Rightarrow S = 1 \cdot 1 = 1$  birlik kv.

$S: 1$  birlik kv.

4. 1 ta boʻla eng kōpi b-h N-1 ta soʻgʻa targʻatishi  
 mumkin va bizda bolalar targʻatgan soʻgʻalar soni harxil bōlishi  
 kerak demak N-1 dan kattā bolmagan N ta

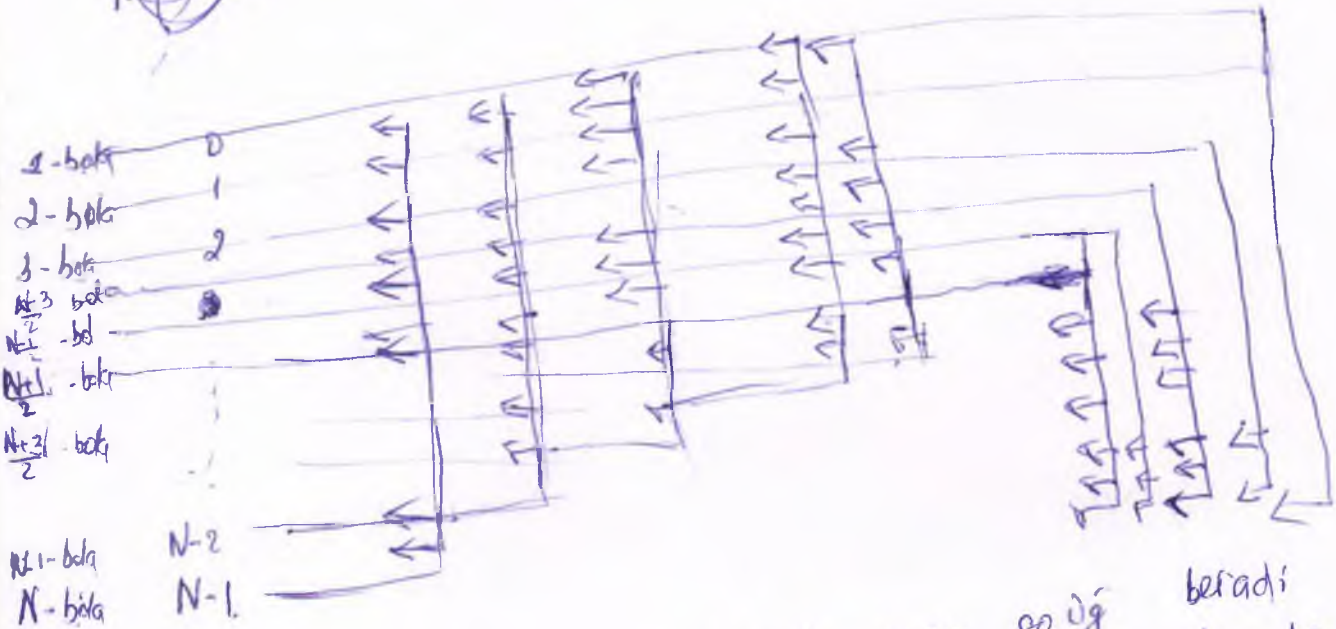
harxil sonni tanlash faqat birkil bōlishi mumkin  
 dani  $\frac{(N-1)N}{2}$  ta  $\frac{N-1}{2} \in N \Rightarrow N \in K$



1-ta bolaga  $\frac{(N-1)N}{2}$ ;  $N = \frac{N-1}{2}$  ta

buholat bōlishi mumkinligini koʻrsatamiz.  

$$N - \frac{N-1}{2} = \frac{N+1}{2}$$



demak bunda N-bola yuqori dagi hammasi soʻgʻ beradi  
 N-1-bola oʻndan yuqoridagi hammasi soʻgʻ beradi va  $\frac{N+1}{2}$  - bola  $\frac{N+1}{2}$  bola  
 buholat  $\frac{N+1}{2}$  gacha taqat taktiraknadi va  $\frac{N-1}{2}$  bolasa  
 esa oʻzidan pastdagi barchaga beradi,  $\frac{N-1}{2}$  bolasa  
 $\frac{N+3}{2}$  dan pastdagi barga,  $\frac{N-3}{2}$  - bola esa  $\frac{N+5}{2}$  dan pastdagi

harchaga, da hozir 2 - bota esa N - bolaga beradi  
shunda hammada  $\frac{N-1}{2}$  tadan sodga bardi,

$$J: N \in \text{toq} \quad \boxed{N \neq 1}$$

$$5) m^3 = n^3 + 13n = 273$$

$$m^3 - n^3 = 13(n - 21)$$

$$(m-n)(m^2 + mn + n^2) = 13(n-21)$$

I hal  
 $m-n = 13k \quad k, m \in \text{butun}$

$$m = n + 13k$$

II hal  $m^2 + mn + n^2 = 13 \cdot \text{?}$

$$(n+13k)^2 + (n+13k)n + n^2 = 13n - 21k$$

$$3n^2 + 38kn + 169k^2 - 21k = 0$$

$$\Delta = (38k)^2 - 12(169k^2 + 21k) = 0$$

$$= \sqrt{-584k^2 - 252k} = t = a^2$$

$$[t_0] \leq 87$$

$$a^2 < 87$$

$$a^2 = 81$$

$$584k^2 + 252k - 81 = 0 \quad k \in \text{butun}$$

$$\Delta = 252^2 - 4 \cdot 584 \cdot 81 = 16(113 \cdot 133 - 14688) \neq k^2 = \emptyset$$

$$a^2 = 64 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 49 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 36 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 25 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 16 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 9 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 4 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 1 \quad \emptyset \neq k^2 \quad \emptyset$$

$$a^2 = 0 \quad \emptyset \leq 0 \quad \boxed{k=0}$$

$$k = -\frac{252}{584} \notin \text{butun} \Rightarrow \emptyset$$

$$m - n = 0$$

$$\underline{m = n}$$

$$n^3 = n^3 + 13n - 273$$

~~13n = 273~~

$$13n = 273$$

$$\boxed{n = 21}$$

2hol  $m^2 + mn + n^2 = 13k$

$$0 = n^2 - 4n^2 + 52k =$$

$$= 52k - 3n^2$$

$$(m-n) \cdot 13k = 13 \cdot (n-21)$$

$$(m-n)k = n-21$$

$$\frac{mk+21}{k+1} = n$$

$$\frac{mk+m+21-m}{k+1} = n$$

$$m + \frac{21-m}{k+1} = n$$

$$m + \frac{21+21k-m-21k}{k+1} = n$$

$$m+21 - \frac{m+21k}{k+1} = n$$

$$\underline{m=21} \quad m+21 - \frac{21+21k}{k+1} = n$$

$$\boxed{n = m = 21}$$

$$n = 21k^2$$

$$m+21 - \frac{21k(k+1)}{k+1} = n$$

$$\boxed{n = m+21-21k}$$

$$m^2 + m^2 + 21m - 21km + m^2 + 441 + 441k^2$$

$$+ 42m - 42km - 882k - 13k = 0$$

$$3m^2 + m(63 - 63k) + 441k^2 - 895k^2 + 441 = 0$$

Ji 21